

# Learning Morphological Productivity as Meaning-Form Mappings

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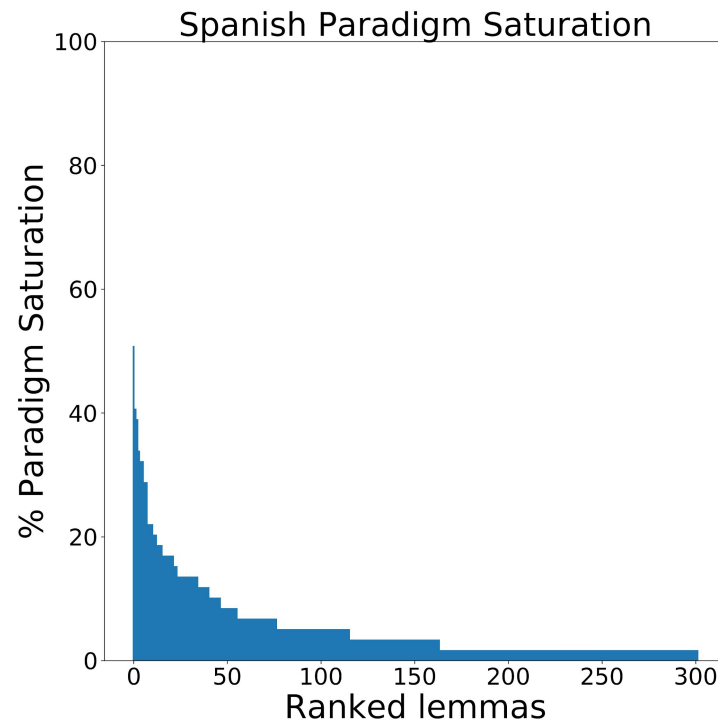
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# The Problem

- Children learn the entirety of verbal morphology from very sparse input
- They have no explicit information as to whether their language is agglutinative or fusional
- This is a mapping problem:  
Semantic features → morphological features



# Our Approach

- We collect child-directed verb forms from CHILDES for English and Spanish
- We annotate these using UniMorph tags
  - UniMorph provides person, number, tense, etc; we consider this an approximation of the child's semantic knowledge
- We apply the Tolerance Principle recursively on the data to pick out larger and smaller patterns (more on this later)

# Outline

- Data + Spanish Basics
- Tolerance Principle + Model
- Results

Data

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# Data: Spanish and English

- **Spanish: 989 inflected forms, 302 lemmas**
  - Sampled from FernAguado corpus by frequency
  - Example:
    - tener V;IND;PRS;2;SG tienes
- **English: 3,953 inflected forms, 1,285 lemmas**
  - Sampled from Manchester, Wells, and Belfast corpora by frequency
  - Example:
    - bake V;V.PTCP;PRS baking
- Frequency is correlated with irregularity in English, but not Spanish (Fratini et al. 2014)

# Spanish Basics

- 3 main classes of verbs: *-ar*, *-ir* and *-er* (defined by infinitive form)
  - *-ar* is largest class (62% of our data vs. 24% *-er* and 14% *-ir*)
  - Mappings often correspond to its behaviour
- Tense and person+number are often indicated separately in an agglutinative fashion
  - E.g., *-ria* = **COND**, *-ra* = **FUT**, *-ba* = **IPFV** (*-ar* verbs), and *-s* = **[2; SG]**
  - So *-rias* = **[COND; 2; SG]**, *-ras* = **[FUT; 2; SG]**, *-bas* = **[IPFV; 2; SG]**

Model

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## The Tolerance Principle (Yang, 2016)

$$e \leq \theta_N = \frac{N}{\ln N}$$

$N$  = the number of words to which are eligible to take a rule

$e$  = the number of those words to which the rule does not apply

Example: 100 past-tense English verbs; 20 don't take **-ed**.  $100/\ln 100 = 21.7$ .  $20 < 21.7$  so **PST** → **-ed** passes the Tolerance Principle

## Model Overview

- GCD application of the Tolerance Principle
- Recursive application of the Tolerance Principle
- Multi-pass application of the Tolerance Principle

# Method: GCD approach

- **Possible suffixes** = substrings of length  $\leq 5$  at the end of an inflected form
  - e.g., possible suffixes of *amar**remos*** are **-remos, -emos, -mos, -os, -s**
- **Possible features realized by each suffix** = all possible subsets of the provided feature set
  - e.g. possible features for **[IND; PRS; 3; SG]** could be **[IND], [IND; PRS], [IND; PRS; 3], [IND; PRS; 3; SG], [PRS], [PRS;3] ...**
- Use a **GCD approach**: find smallest feature-set that maps to a suffix
  - Do a pass of the TP from feature-sets to suffixes
  - For each suffix that was mapped to, find the intersection of all features that mapped to it
  - Keep adding features by frequency until a mapping from the features to suffix passes

## Example: GCD approach using the Tolerance Principle

In Spanish, **-mos** = **[1;PL]**, which we obtain as follows:

1. Do a pass of the TP from feature-sets to suffixes
  - This yields mappings such as **[1; PL]** = **-mos**, **[1; PL; FUT]** = **-ramos**, **[1; COND]** = **-riamos**
  - Some of these (e.g. **[1;COND]**) are underspecified, others are overspecified
  - We cannot learn agglutinativity from these mappings alone

## Example: GCD approach using the Tolerance Principle

2. For each suffix that was mapped to, find the intersection of all features that mapped to it
  - For **-mos**, say this suffix was mapped to by **[1;PL]**, **[IND; PRS; 1; PL]**, and **[POS; IMP; 1]**
  - The intersection of these gives **[1]** = **-mos**, which won't pass the TP

## Example: GCD approach using the Tolerance Principle

3. Keep adding features by frequency until a mapping from the features to suffix passes
  - The second-most frequent feature is **PL**, and **[1; PL] = -mos** passes

# Method: Recursive Application of the TP

- We learn the broadest mappings first
  - e.g. in Spanish, **[3; SG]** = “”
- Then we recurse on the exceptions to these broad mappings to learn narrower mappings
  - e.g. in Spanish, **[3; SG]** = “” except **[3; SG; PFV]** = -o
  - We learn the latter mapping by recursively applying the TP to the verbs that fail to be correctly inflected by **[3; SG]** = “”
- We memorize verbs that remain exceptions after recursion
  - In Spanish, we learn narrow mappings such as **[3; SG; PFV]** = -o and stem conditioned endings such as the imperfective
  - In both cases, we can predict the rule we use based on properties of the lemma or features
  - However, we can't do the same for *ser*, so we memorize its inflected forms

# Method: Multi-Pass Application of the TP

- In agglutinative languages, more frequent features are realized closer to the end of the inflected form
  - e.g. in Spanish, person & number are always realized at the end and are most common
- We consider feature categories (person, number, mood, tense, aspect) in order of decreasing frequency
- At each pass, we constrain GCD mappings to the given feature category/categories and recurse on these before moving to the next one
  - In Spanish, we learn person-number endings and their productive exceptions first.
  - This includes **[3; SG]** = “” and **[3; SG; PFV]** = **-o**, which is learned via recursion at this pass
- We remove the suffixes we’ve learned at a given pass from the inflected forms before moving on to the next pass
  - After removing Spanish person-number endings, we learn mappings such as **[COND]** = **-ria**



## Model Overview

At each pass, constrained by feature categories:

- Do a GCD pass of the Tolerance Principle

- Recurse on exceptions

- Memorize anything left

# Results

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# Results: English

Broad Mappings				
Features	Defau.	Alternations	Ct.	Ex.
<b>First Pass</b>				
PRS	∅		2573	<i>walk</i>
<b>Second Pass</b>				
3	∅		1717	<i>walk</i>
2	∅		571	<i>walk</i>
1	∅		554	<i>walk</i>
<b>Third Pass</b>				
PL	∅		1454	<i>walk</i>
SG	∅		1422	<i>walk</i>
<b>Fourth Pass</b>				
NFIN	∅		22	<i>walk</i>

Narrow Mappings				
Features	Defau.	Alternations	Ct.	Ex.
<b>First Pass</b>				
PTCP, PRS	ing	e → ing	643	<i>pleasing</i>
3 SG PRS	s		372	<i>walks</i>
<b>Second Pass</b>				
3 PL PST	ed	y→ied,e→ed	367	<i>pleased</i>
3 SG PST	ed	y→ied	139	<i>tried</i>
2 SG PST	ed	y→ied,e→ed	203	<i>walked</i>
1 SG PST	ed	y→ied,d→t	136	<i>built</i>
1 PL PST	ed	y→ied	67	<i>cried</i>

# Results: Spanish

Broad Mappings				
Features	Default	Alterns.	Ct.	Ex.
<b>First Pass</b>				
3 SG	∅		227	<i>ama</i>
3 PL	n		103	<i>aman</i>
1 PL	mos		51	<i>amamos</i>
2 PL	is		10	<i>amais</i>
PRS 1 SG	o		163	<i>amo</i>
PRS 2 SG	s		129	<i>amas</i>
<b>Second Pass</b>				
IND	∅		651	<i>ama</i>
IMP	∅		127	<i>ama</i>
NFIN	r		146	<i>amar</i>
COND	ria		16	<i>amaria</i>
<b>Third Pass</b>				
PRS	∅		492	<i>ama</i>
FUT	ra		20	<i>amara</i>
<b>Fourth Pass</b>				
IPFV	ia	a→aba	65	<i>amaba</i>

Narrow Mappings				
Features	Default	Alterns.	Ct.	Ex.
<b>First Pass</b>				
SBJV PRS 3 SG	e	i → a	13	<i>ame</i>
POS IMP 3 SG	e	i → a	14	<i>ame</i>
IND PST 3 SG PFV	o		72	<i>amo</i>
SBJV PRS 3 PL	an		2	<i>coman</i>
POS IMP 3 PL	an		2	<i>coman</i>
IND PST 3 PL PFV	ron		23	<i>amaron</i>
POS IMP 1 PL	emos		3	<i>amemos</i>
SBJV PRS 1 PL	emos		3	<i>amemos</i>
POS IMP 2 PL	d		2	<i>amad</i>
SBJV PRS 1 SG	e	i → a	14	<i>ame</i>
IND PST 1 SG PFV	e	i → i	18	<i>ame</i>
COND 2 SG	rias		2	<i>amarias</i>
SBJV PRS 2 SG	es	i → as	33	<i>ames</i>
IND FUT 2 SG	ras		3	<i>amaras</i>
IND PST 2 SG IPFV	ias		9	<i>comias</i>
IND PST 2 SG PFV	ste		10	<i>amaste</i>
<b>Second Pass</b>				
IND FUT 1 PL	re		2	<i>amaremos</i>

# Discussion + Future Work

- Segmentation and generation
  - Our model may be extended to be competitive on computational linguistics and NLP morphological tasks
- Developmental plausibility
  - Our model learns rules in a similar order to children
  - Does it exhibit U-shaped development?
- Non-verbal morphology
  - Derivational or German nouns

# Thank you!!

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